NUMERICAL SIMULATION AND ANALYSIS OF THE VERTICAL AND DOUBLE PIPE SOIL-AIR HEAT EXCHANGER

by

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A quasi-3-D soil-air heat and mass transfer model was established to simulate the process of heat and moisture exchange in the vertical and double soil-air heat exchanger. At the same time, the heat and moisture exchange were considered in the model, and the air-flow parameter equation and heat transfer control equation were combined. The MATLAB was used for the calculation procedure, and the model was solved using an iterative method. The average relative error of the numerical calculation was less than 2\%. Moreover, the heat exchanger performance influence factors were validated. The simulation results showed that: with the lengthening of the heat exchanger, the smaller the air-flow, the shorter the running time, the air temperature and moisture content at the outlet of the heat exchanger were lower, the cooling and dehumidification effect were more obvious. However, the magnitude of change gradually decreased, and finally stabilized.

Key words: vertical-double pipe, soil-air heat exchanger, numerical analysis, dehumidification

Introduction

The temperature of soil is not constant, is lower than the temperature of outdoor air in summer, and is higher than temperature of outdoor air in winter. Soil is one of the good and free cold/heat sources for air conditioning. Ground source heat pump has been investigated experimentally and numerically in the past few decades [1]. The fresh air can also be cooled or heated by the underground soil, and transferred into the building by mechanical or inductive ventilation system. It is called soil-air heat exchange system. Internationally, soil-air heat exchange systems are applied to a large number of hospitals [2], and greenhouses [3]. Locally, they are also extensively applied in theaters, hall [4], greenhouse [5, 6], subway station [7], museum [8], office [9], building, etc. Research studies show that they can improve the indoor air temperature, have good benefits for energy conservation and environmental protection. However, soil-air heat exchanger is always used for cooling the air, and the soil-air heat exchanger generally consists of horizontal buried tube type and natural tunnel.

A vertical and double pipe soil-air heat exchanger [10] is developed, and tested the cooling and moisture removing effect of this type of heat exchanger. Figure 1 is the physical model of the soil-air heat exchanger. The soil-air heat exchanger is made of double tubes. The outer tube is rock hole, with a diameter of 130 mm. The inner tube is a PVC pipe, and

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the diameter is 75 mm, and is supported by a bracket with height of 2 m at the bottom of rock hole. While the heat exchanger is working, fresh air is introduced by the fan into the ring cavity of soil-air heat exchanger, and sent out by inner tube after the heat and moisture transfer with the rock wall. In summer, the heat and mass transfer process of soil-air heat exchanger is as follows: the hot and wet air-flow into the ring cavity of heat exchanger, and is cooled by the rock wall. When the temperature of rock wall is lower than the wet air dew point temperature, wet air would condense and heat and mass transfer will occur between air and rock wall. When air-flows to the bottom of the heat exchanger, it will be sucked into the inner tube and conducted heat transfer with inside wall of the tube. Heat and moisture transfer between air and rock will decrease the air temperature in the heat exchanger, and in turn, the temperature of rock face will be influenced by the air, and the changes of rock face temperature will affect the internal temperature distribution of rock mass. That is, the hot fresh air will influence the temperature distribution in the rock mass. The daily amplitude and yearly amplitude of inlet air temperature will affect the heat exchange process, and interlocking delay phenomenon exists in the whole heat transfer process. Therefore, heat and mass exchange between air and soil is a complex and unsteady process.

In order to predict the heat and mass exchange capacity of the vertical and double pipe soil-air system, this paper established the heat and mass transfer mathematical model of the heat exchanger, and carried out numerical simulation, it provided a theoretical support for the application of the heat exchanger in engineering field. Local and international scholars have done a lot of research on the soil-air heat transfer model. Paepe et al. [11] established a calculation model, the model considered the fluctuations of the air temperature and the changes of soil temperature and their effect on the heat convection. In his research, the soil-air heat exchanger is segmented, and outlet air temperature is obtained by piecewise calculation. Scholars in Shandong Institute of Architectural Design, Mou [12] established the semi-infinite body steady-state heat transfer model under the boundary conditions of constant heat flux. The model can predict the supply air temperature under the most unfavorable conditions of air conditioning system, but it cannot be used to obtain the operation status of the system in the fluctuation of meteorological parameters, and the algorithm cannot be used to calculate the annual operation status either. A 3-D unsteady heat transfer process of the soil-air heat exchanger under dry condition is solved by Song and Zhu [13] of Tsinghua University, and the influence of various design factors on the heat exchange system are analyzed. South China University of Technology, Wu et al. [14] dynamically simulated soil-air buried tube heat exchange system based on turbulence model and soil source conduction equation, using the method of temperature field superposition. Obtained dynamic changes of the air temperature at outlet of the buried pipe, and studied the effect of factors such as buried pipe length (flow rate, pipe diameter) on air temperature at outlet of heat exchanger. Zhang et al. [15] analyzed the influences of tunnel length, air velocity and depth on heat transfer between underground tunnel and air in winter through the 3-D nu-
merical simulation. All the previous models did not consider the influence of air condensation on the heat exchange process and on the air humidity at outlet of heat exchanger. Jacovides and Mihalakakou [16] from the University of Athens established a mathematical model to simulate the temperature distribution of soil-air thermal exchange system, and did research on the cooling and heating capacity of the buried pipe system. The model not only considered the heat and mass exchange in the soil-air heat exchange system, but also considered the thermal stratification naturally. A 2-D model of the buried heat exchanger and 3-D transient heat exchange model were established in cylindrical co-ordinates, and showed consistency between the simulations and the experiments. Xia et al. [17] studied the heat exchange process of a tunnel ventilation system in a school, and built a quasi-3-D heat and mass transfer model between soil and air, carried out numerical simulation considering condensate in the heat and mass transfer process, and finally validated the simulation results with the measured data. Whether air condensation was considered in the heat transfer process, or whether the air humidity distribution was obtained by simulation, most of mathematical models and the experiments were both aimed at traditional soil-air heat exchange system. In this paper, a heat and mass exchange model set-up would be for a new vertical double pipe soil-air heat exchanger which was used for air dehumidification, it could predict the cooling and dehumidifying capacity.

**Materials and methods**

**Hypothesis of soil-air heat transfer model**

Heat transfer is a complex and unsteady process between air and soil in soil-air heat exchanger. It needs a long time to compute, and the geometry and physical conditions involved in the process are very complex. In order to analyze easily, it is necessary to simplify the problem: Ignoring the heat transfer between the air in the inner duct and the air in the ring cavity through the wall of inner duct, assuming that thermal insulation performance of the inner duct is good, only considering the heat and mass exchange between the air in ring cavity and rock face. Supposing air temperature at similar cross-section is the same, only considering the change of air temperature along the flow direction. Assuming the initial temperature of soil is not continuously changing with depth, and remains unchanged within 1 m. The inlet air temperature and humidity is not continuously changing over time, and remains unchanged within 1 hours. The calculation model of soil-air heat exchanger is shown in fig. 2. The control equation and boundary conditions of soil-air heat exchange are listed. Two cases: condensation and no condensation were considered separately in the thermal balance equation of air.

**Soil-air heat transfer mathematic model**

Heat conduction equation in the soil shown as:

\[
\frac{\partial t}{\partial \tau} = a \left[ \frac{\partial^2 t}{\partial r^2} + \frac{1}{r} \frac{\partial t}{\partial r} + \frac{\partial^2 t}{\partial z^2} \right]
\]
Air heat balance equation [18, 19]

When there is no condensed water on the rock face, air heat balance is shown as:

\[ Gc \frac{\partial T}{\partial z} = h(t_{r=r_2} - T)u \]  

(2)

When there is condensed water on the wall, air heat balance is shown as:

\[ G \left[ c \frac{\partial T}{\partial z} + 622 \gamma \frac{\partial \varphi}{\partial z} - \frac{e^{f(T)}}{B - e^{f(T)}} \right] = h(t_{r=r_2} - T)u \]  

(3)

\[ \varphi = \frac{d}{d_b} \cdot 100\% \]  

(4)

\[ d_b = \frac{622 p_{q,b}}{B - p_{q,b}} \]  

(5)

\[ F(T) = \ln(p_{q,b}) = \frac{C_1}{T} + C_2 + C_3 T + C_4 T^2 + C_5 T^3 + C_6 \ln(T) \]  

(6)

where \( C_1 = -5800.2206, C_2 = 1.3914993, C_3 = -0.04860239, C_4 = 0.41764768 \times 10^{-4}, \) 
\( C_5 = -0.14452093 \times 10^{-7}, \) and \( B [\text{Pa}] \) – the atmospheric pressure.

Boundary conditions shown as:

\[ -\lambda \left. \frac{\partial t(r, \tau)}{\partial r} \right|_{r=r_2} = h(T - t_{r=r_2}) \]  

(7)

Initial conditions shown as:

\[ t_{r=0} = t_0 \]  

(8)

\[ T|_{r=0,z=0} = T_1 \]  

(9)

\[ d|_{r=0,z=0} = d_1 \]  

(10)

where \( t_0 [\text{℃}] \) is the initial temperature of soil, \( T_1 [\text{K}] \) – the inlet air temperature, and \( d_1 [\text{gkg}^{-1} \text{dry air}] \) – the inlet air humidity ratio.

Meshing

Calculation areas are selected in two parts: soil section, the annular air cavity between soil and inner pipe. The category of node is different in different areas. The grids which are divided in cylindrical co-ordinates are shown in fig. 3. Soil (rock) area (shadows) is 2-D unsteady heat conduction, thus, meshes are along the radial and vertical direction. In the region of the annular air cavity, the air temperature is assumed constant along the radial, the grids are divided vertically.
Model solution

According to the control equations, the heat transfer in the soil is 2-D transient heat conduction, and it is difficult to solve. In order to simplify the solving process, the calculation area along the vertical direction is divided into a number of adiabatic units. The shorter each unit is, the more accurate of the calculating results are. In each adiabatic unit, it is assumed that the soil and air temperature are constant along the vertical direction and the heat conduction in the vertical direction is ignored.

The specific process of calculation is shown in fig. 4. Firstly, at a given time, the node in the first unit is calculated, the result of the computation is as the boundary conditions of the second unit, and then the node in the second unit will be calculated. The rest can be calculated in the same manner, all the grid nodes in all the units will be calculated, and then into the calculation of next level.

The governing equation underwent discretion within each computing element with heat conduction along z-axis was being neglected. The first-order derivative of temperature vs. space was expressed with forward difference while the second-order derivative with central difference. The first-order derivative of temperature vs. time was expressed with explicit difference. It is necessary to make sure the coefficients of all the items in the discrete equation are \( \Delta \tau \leq 0 \), or calculated values would fluctuate at different moments and conclusions against the law of thermodynamics would be drawn.

It has been assumed that the inlet air temperature is constant within 1 hours. In order to simplify the calculation, take a time step is \( \Delta \tau = 10 \text{ s} \). In order to ensure the accuracy of the calculation result, the mesh in the soil region is \( \Delta r = 0.05 \text{ m} \).

The soil area is decomposed into multiple units which are adiabatic rocks with each other along the vertical direction, and taking the length of each unit \( \Delta z = 1 \text{ m} \). It does not only ensure the precision of the calculation, but also accelerate the speed of calculation.

Calculation program was compiled using MATLAB language. In the program, the change of the annual outdoor air temperature and air-flow rate, the distance between node \( \Delta r \), time step \( \Delta \tau \), the length of the unit \( \Delta z \) were the known conditions. When the program was operating, through the input of several parameters such as operation time, the size of soil-air heat exchanger (inner tube diameter, rock hole diameter, rock hole depth), the density and thermal conductivity and specific heat of the soil, specific heat of the air, the temperature of each node in each unit can be calculated. The flow chart of the calculation program was shown in fig. 5.

Experimental verification

In order to validate the rationality of the model, experimental analysis has been done. The soil-air heat exchange device is located in the Lab Building of Chongqing University,
which is shown in fig. 6. The mathematic model was verified through comparing the experimental results and simulation results.

The main geometric parameters and operation parameters of the soil-air heat exchanger are shown in tab. 1. Running time was from July 28 8:00 to August 11 23:00, continuously running 24 hours a day.

![Figure 5. The flow chart of calculation program](image)

Output the results: in the time $\Delta \tau$, during the operation time $\tau$, air temperature and humidity ratio and the soil temperature

![Figure 6. The room for inducing and exhausting air of soil-air heat exchanger](image)
The calculations of numerical simulation used heat and mass transfer model of soil-air heat exchanger. The basic size and material physical parameters of the heat exchanger are shown in tab. 2, and the initial temperature of the soil are shown in tab. 3. Hourly outdoor air temperature and humidity ratio are input parameters, which are shown in fig. 7. Air-flow rate in the heat exchanger is 125 m$^3$/h.

Table 1. Operating parameters in summer

<table>
<thead>
<tr>
<th>Parameter</th>
<th>$r_2$</th>
<th>$r_1$</th>
<th>$z$</th>
<th>$G$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>0.065</td>
<td>0.0375</td>
<td>23</td>
<td>125</td>
</tr>
</tbody>
</table>

Table 2. Heat exchanger size and soil physical parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>$r_2$</th>
<th>$r_1$</th>
<th>$z$</th>
<th>$\lambda$</th>
<th>$\rho$</th>
<th>$c$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>0.065</td>
<td>0.0375</td>
<td>23</td>
<td>2.035</td>
<td>2400</td>
<td>0.921</td>
</tr>
</tbody>
</table>

Table 3. Initial soil temperature

<table>
<thead>
<tr>
<th>Depth, [m]</th>
<th>Temperature, [°C]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>26.87</td>
</tr>
<tr>
<td>2</td>
<td>24.15</td>
</tr>
<tr>
<td>3</td>
<td>22.08</td>
</tr>
<tr>
<td>4</td>
<td>20.67</td>
</tr>
<tr>
<td>5</td>
<td>19.81</td>
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<tr>
<td>6</td>
<td>19.38</td>
</tr>
<tr>
<td>7</td>
<td>19.23</td>
</tr>
<tr>
<td>8</td>
<td>19.25</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Depth, [m]</th>
<th>Temperature, [°C]</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>19.36</td>
</tr>
<tr>
<td>10</td>
<td>19.5</td>
</tr>
<tr>
<td>11</td>
<td>19.63</td>
</tr>
<tr>
<td>12</td>
<td>19.74</td>
</tr>
<tr>
<td>13</td>
<td>19.83</td>
</tr>
<tr>
<td>14</td>
<td>19.88</td>
</tr>
<tr>
<td>14-25</td>
<td>19.91</td>
</tr>
</tbody>
</table>

Figure 7. The weather data of Chongqing

Results

Validation results

A comparison of the measured results and simulated results are shown in figs. 8 and 9. The variation rule of measured and simulated values at the bottom of hole are consistent during the operation of the soil-air heat exchanger. The average air temperature measured at the bottom of the rock hole was 21.36 °C, average air temperature simulated at the bottom of the hole was 21.74 °C, the difference was about 0.3 °C, and the error between the simulation results and the experimental results during all the running time was less than 8%. The measured average air moisture content at the bottom of the rock hole was 16.78 g/kg (dry air), simulated average air moisture content at the bottom of the hole was 16.46 g/kg (dry air), the simulation results was lower than the actual result of 0.3 g/kg (dry air), and the error between the simulation results and the experimental results during all the running time was less than 10%.

The influence of the heat exchanger depth on its performance

The air parameters at the outlet were different for different heat exchanger depths. In order to investigate the influence of the heat exchanger depth on its performance, the exit
air temperature and humidity ratio were obtained by simulation when the depth of the heat exchanger was 5 m, 10 m, 15 m, 20 m, and 25 m. Therefore, the cooling and dehumidification ability of the heat exchanger were calculated as in figs. 10 and 11.

As it can be seen from fig. 10, the heat exchanger has apparent cooling effect. The cooling ability was strengthened with the increase of the depth of the heat exchanger. However, with the increase of depth of the heat exchanger, the rise of cooling ability seems to be fairly smooth. Moreover, with the increase of operation time, the decrease of the inlet air temperature, the heat exchanger’s cooling ability gradually became smaller. In the running time, 6 days in a row, for the heat exchanger with the depth of 5 m, 10 m, 15 m, 20 m, 25 m, the maximum temperature decrease were 10.3 °C, 11.8 °C, 13.1 °C and 14.1 °C and 14.7 °C, respectively.

From fig. 11, it can be seen that the heat exchanger had obvious dehumidifying effect, the dehumidification capacity increased with increasing depth of the heat exchanger. With the increase of operation time, inlet air humidity ratio decreased, and desiccant quantity decreased. In the running time 6 days in a row, for the heat exchanger with the depth of 5 m, 10 m, 15 m, 20 m, 25 m, the maximum desiccant quantity were 3.9, 6.3, 7.5, 8.0, 8.2 g/kg (dry air).
The influence of the air volume flow rate on the performance of the heat exchanger

Air volume flow rate influence air velocity in underground heat exchanger, in turn, affecting the heat transfer coefficient between soil and air convection, subsequently, they can affect cooling and dehumidifying capacity of heat exchanger. Heat transfer effects were discussed when air volume flow rate were 50, 100, 150, 200, 250 m$^3$/h and heat exchanger size was constant.

As it can be seen from fig. 12, the drop of temperature decreased with increasing air-flow rate, increased with increasing inlet air temperature. The cooling ability decayed with the increase of operation time. The greater the air volume flow rate was, the faster of cooling ability decayed. When air-flow rate were 50, 100, 150, 200, 250 m$^3$/h, the maximum temperature drop of the heat exchanger were 15.4, 15.2, 14.5, 13.7, 12.9 °C. From fig. 13, it can be seen that the dehumidification quantity is reduced with the increase of air-flow rate, increased with the increase of the inlet air moisture content, and reduced with the increase of operation time. The greater the air volume flow rate was, the faster of the dehumidifying capacity decay. When air-flow rate was 50, 100, 150, 200, 250 m$^3$/h, the maximum dehumidification capacity of the heat exchanger were 9.0, 8.8, 8.2, 7.8, 7.4 g/kg (dry air).
In this paper, the soil-air heat exchanger is used not only for cooling of the fresh air, but also for air dehumidification. They could be used to cool or pre-dehumidify the fresh air without additional cooling effects. So the designed soil-air heat exchangers are buried deeper that other earth-tube [20] or straight and spiral earth-air heat exchangers [21]. In order to investigate the cooling and dehumidifying capacity, the heat and mass transfer model was established and numerically discretized and solved in this paper. The mathematical heat and mass transfer model proved correct through the comparison of numerical results and experiment results. The result indicates that the soil-air heat exchanger has good cooling and also dehumidification ability. The cooling ability is similar to the previous research. The fresh air temperature drops significantly and decreases until the air temperature becomes equal to soil temperature. In this paper, the maximum temperature drop is about 16 ℃. In [22], the maximum temperature drop is about 20.7 ℃. The temperature difference between inlet and outlet is related to the inlet air temperature, air volume and the length of the heat exchanger. The dehumidification capacity
of vertical soil-air heat exchanger is better than the horizontal soil-air heat exchanger. That because the soil temperature is lower and more stable in the depth of 23 m than 1 m. The maximum water condensation of a horizontal soil-air heat exchanger, on the summer day is only 0.006 kg [23]. In addition, the relationship of the heat exchanger depth (air volume, operation time) and the exit air temperature (humidity ratio) was obtained by the numerical simulation. The simulation results show that the temperature drop or dehumidification capacity increases with the increase of heat exchanger length and increases with the decrease of air volume flow rate and increases with the operating time. Moreover, the amplitude of the variation gradually become flatter and flatter. The simulation results can supply a theory basement for the design of vertical double pipe soil-air heat exchanger applied to different region. In this paper, the mathematic model is not considering the influence of underground flow. And the thermal properties of soil will also be different because of the multi-phase nature of the soil. Other types of vertical earth-air heat exchanger can be studied for better cooling and dehumidification capacity. Further investigation into the impact of these factors is therefore necessary.

Acknowledgment

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Nomenclature

\( a \) – thermal diffusivity of soil, 
\( (= 0.33 \times 10^{-2}, [m^2 h^{-1}]) \)
\( c \) – specific heat of air, \([kJkg^{-1}K^{-1}]\)
\( d \) – air humidity ratio of air, \([kg/(kg dry air)^{-1}]\)
\( d_b \) – air humidity ratio of saturated air, \([kg/(kg dry air)^{-1}]\)
\( d_e \) – equivalent diameter, \((= 2r_2 - 2r_1), [m]\)
\( G \) – ventilation rate, \([kg/s]\)
\( h \) – convective heat transfer coefficient \(\left[= \left(0.045 \lambda Re^{0.8}/d_e\right)\right], [Wm^{-2}K^{-1}]\)
\( p_{q,h} \) – the partial pressure of saturated steam, \([Pa]\)
\( Re \) – Reynolds number \(\left[= Gd/(\pi(r_2^2 - r_1^2)v)\right], [-]\)
\( r_1 \) – the outside radius of inner air duct, \([m]\)
\( r_2 \) – the radius of rock hole, \([m]\)
\( r_3 \) – the adiabatic boundary of soil, \([m]\)
\( r \) – the distance from some point to the hole center in the soil radial direction, and \(r \geq r_3, [m]\)

\( T \) – air temperature, \([^\circ C]\)
\( t \) – soil temperature, \([^\circ C]\)
\( u \) – the perimeter of ring cavity cross-section, \([m]\)
\( z \) – the distance from some point to ground in the depth direction of the hole, \([m]\)

Greek symbols

\( \gamma \) – gasification latent heat, \([J]\)
\( \lambda \) – thermal conductivity of soil, \([Wm^{-1}K^{-1}]\)
\( \nu \) – coefficient of kinematic viscosity of air, \([m^2s^{-1}]\)
\( \rho \) – density, \([kgm^{-3}]\)
\( \tau \) – operation time, \([h]\)
\( \phi \) – air relative humidity, \([\%]\)

References

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